



Notes:

- Each question carries 30 marks.
- Figure on the right of each question indicate marks for respective question.

Time: 1 Hour

Full Marks: 60

Answer any two questions including question no.1

- Explain why the value of wavefunction is zero outside infinite potential well? (5)
  - From time independent Schrodinger's equation, deduce the expression of wave function  $\Psi(x)$  for an electron trapped in an infinite potential well shown in Fig :Q1(b) mentioning the main considerations while deriving the solution. (13)

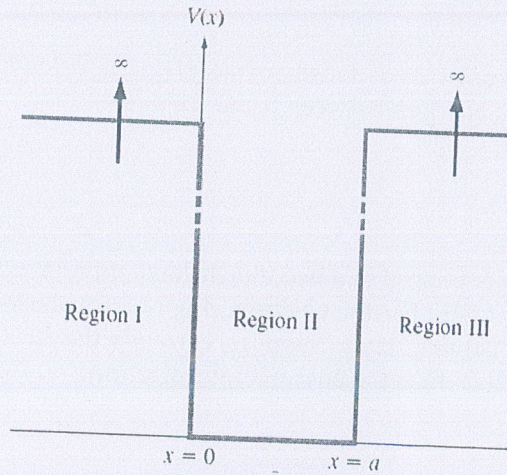


Fig : Q1(b)

- Consider the following figure at Fig : Q1(c). The probability of finding a particle at a distance  $d$  in region II compared with that at  $x = 0$  is given by  $\exp(-2k_2d)$ . Consider an electron traveling in region I at a velocity of  $10^5$  m/s incident on a potential barrier whose height is three times ( $3\times$ ) the kinetic energy of the electron. Calculate the probability of finding the electron at a distance  $d$  compared with  $x = 0$  where  $d$  is ( a )  $10 \text{ \AA}$  and ( b )  $100 \text{ \AA}$  into the potential. (12)

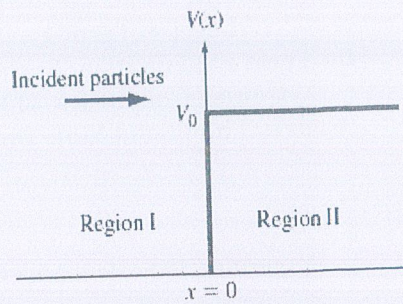


Fig : Q1(c)

2. a. Considering a free electron confined to a three-dimensional infinite potential well, derive the expression of density of states per unit volume as a function of energy ( $g(E)$ ) and show that (14)

$$g(E) = \frac{4\pi(2m)^{3/2}}{h^3} \sqrt{E}$$

- b. Using the expression of density of states ( $g(E)$ ), calculate the density of states per unit volume with energies between 0 and 1 eV. (8)

- c. An electron is trapped in a two dimensional infinite well of dimension  $a = 5 \text{ \AA}$  in both  $x$  and  $y$  direction. For the electron, Fig : Q2(c) shows the two dimensional array of allowable quantum states. Suppose, currently the electron is the state A as marked in the Fig : Q2(c). Find the energy of the electron. (8)

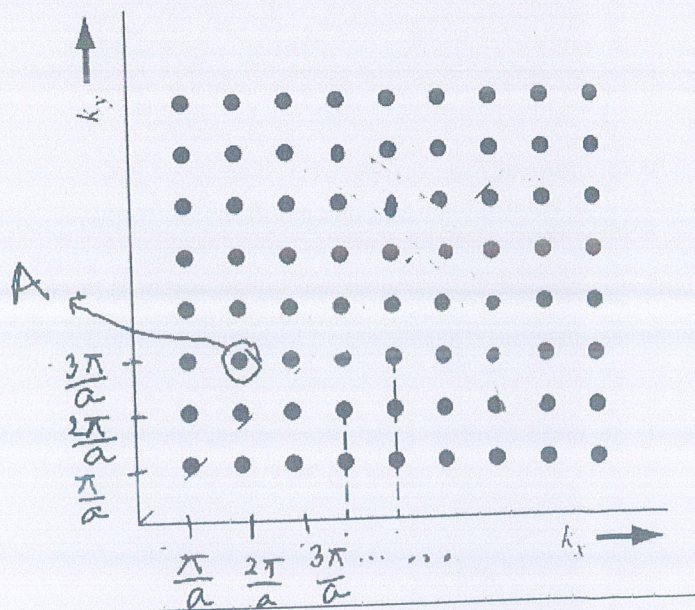


Fig : Q2(c).

3. a. Draw a diagram of Electron energy vs interatomic distance for  ${}_6\text{C}$  atom and show how conduction and valence band forms by combination and splitting of 2s and 2p states. (10)  
(Indicate no of states and no of electrons in the diagram)
- b. Write down the expression for fermi probability function (  $f(E)$  ) and qualitatively plot it against energy (E). Also, show how the graph changes with the variation of temperature. (8)
- c. Assume the Fermi energy level is 0.30 eV below the conduction band energy  $E_c$ . Assume  $T = 300$  K. (a) Determine the probability of a state being occupied by an electron at  $E = E_c + kT/4$ . (b) Repeat part (a) for an energy state at  $E = E_c + kT$ . (12)

--THE END--